

$$[1] \quad \frac{\partial}{\partial t} \frac{\partial L}{\partial [\text{travel}]} - \frac{\partial L}{\partial [\text{travel}]} = (Vf + Vb)Kf L_a \sin(\text{pitch}(t))$$

$$[2] \quad T_1^{mc} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(\text{elev}(t)) & \sin(\text{elev}(t)) & Lw\cos(\text{elev}(t)) \\ 0 & \sin(\text{elev}(t)) & \cos(\text{elev}(t)) & Lw\sin(\text{elev}(t)) \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$[3] \quad T_1^{hb} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(\text{elev}(t)) & \sin(\text{elev}(t)) & Lacos(\text{elev}(t)) \\ 0 & \sin(\text{elev}(t)) & \cos(\text{elev}(t)) & Lasin(\text{elev}(t)) \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$[4] \quad T_{hb}^f = \begin{bmatrix} \cos(\text{pitch}(t)) & 0 & \sin(\text{pitch}(t)) & Lh\cos(\text{pitch}(t)) \\ 0 & 1 & 0 & 0 \\ \sin(\text{pitch}(t)) & 0 & \cos(\text{pitch}(t)) & Lhsin(\text{pitch}(t)) \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$[5] \quad T_{hb}^b = \begin{bmatrix} \cos(\text{pitch}(t)) & 0 & \sin(\text{pitch}(t)) & Lh\cos(\text{pitch}(t)) \\ 0 & 1 & 0 & 0 \\ \sin(\text{pitch}(t)) & 0 & \cos(\text{pitch}(t)) & Lhsin(\text{pitch}(t)) \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$[6] \quad \begin{aligned} T_{mc} &= T_0^1 T_1^{mc} \\ T_{hb} &= T_0^1 T_1^{hb} \\ T_f &= T_{hb} T_{hb}^f \\ T_b &= T_{hb} T_{hb}^b \end{aligned}$$

$$[7] \quad \begin{aligned} pe_{mc} &= mc g p_z^{mc} \\ pe_f &= mf g p_z^f \\ pe_b &= mf g p_z^b \end{aligned}$$

$$[8] \quad \begin{aligned} ke_{mc} &= 0.5mc \left( v_x^{mc2} + v_y^{mc2} + v_z^{mc2} \right) \\ ke_f &= 0.5mf \left( v_x^{f2} + v_y^{f2} + v_z^{f2} \right) \\ ke_b &= 0.5mb \left( v_x^{b2} + v_y^{b2} + v_z^{b2} \right) \end{aligned}$$

$$\begin{aligned}
ke &= ke_{mc} + ke_f + ke_b \\
pe &= pe_{mc} + pe_f + pe_b \\
L &= ke - pe
\end{aligned}$$

[9]

$$\frac{\partial}{\partial t} \frac{\partial L}{\partial [elev]} - \frac{\partial L}{\partial [elev]} = L_a Kf (V_f + V_b)$$

[10]

$$\frac{\partial}{\partial t} \frac{\partial L}{\partial [travel]} - \frac{\partial L}{\partial [travel]} = (V_f + V_b) Kf L_a \sin(\text{pitch}(t))$$

[11]

$$\frac{\partial}{\partial t} \frac{\partial L}{\partial [pitch]} - \frac{\partial L}{\partial [pitch]} = Kf (V_f - V_b) L_h$$

[12]

$$\begin{aligned}
F_1(\text{elev}, \text{pitch}, \text{travel}) &= G_1(V_f, V_b) \\
F_2(\text{elev}, \text{pitch}, \text{travel}) &= G_2(V_f, V_b) \\
F_3(\text{elev}, \text{pitch}, \text{travel}) &= G_3(V_f, V_b)
\end{aligned}$$

[13]

$$\begin{aligned}
\dot{\varepsilon} &= R(\varepsilon, p, \lambda, V_f, V_b) \\
\dot{p} &= R(\varepsilon, p, \lambda, V_f, V_b) \\
\dot{\lambda} &= R(\varepsilon, p, \lambda, V_f, V_b)
\end{aligned}$$

[14]

$$Q = \left[ \varepsilon = 0, p = 0, \lambda = 0, \dot{\varepsilon} = 0, \dot{p} = 0, \dot{\lambda} = 0, V_f = V_q, V_b = V_q \right]$$

[15]

$$V_q = \frac{g(Lwmc - 2Lamf)}{2Kf}$$

[16]

$$\begin{bmatrix} \dot{\varepsilon} \\ \dot{p} \\ \dot{\lambda} \\ \dot{\varepsilon} \\ \dot{p} \\ \dot{\lambda} \\ \dot{\zeta} \\ \dot{\gamma} \end{bmatrix} = A \begin{bmatrix} \varepsilon \\ p \\ \lambda \\ \varepsilon \\ p \\ \lambda \\ \zeta \\ \gamma \end{bmatrix} + B \begin{bmatrix} V_f \\ V_b \end{bmatrix}$$

[17]

$$A = \begin{bmatrix} 0.00 & 0.00 & 0.00 & 1.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 & 0.00 & 1.00 & 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 1.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.00 & 0.60 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 1.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 1.00 & 0.00 & 0.00 & 0.00 & 0.00 & 0.00 \end{bmatrix}$$

$$B = \begin{bmatrix} 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.15 & 0.15 \\ 1.02 & 1.02 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \\ 0.00 & 0.00 \end{bmatrix}$$

[18]

$$[19] K = \begin{bmatrix} 18.30 & 10.14 & 17.55 & 12.02 & 3.52 & 26.00 & 3.54 & 1.12 \\ 18.30 & 10.14 & 17.55 & 12.02 & 3.52 & 26.00 & 3.54 & 1.12 \end{bmatrix}$$